

Fuzzy Temporal Non-monotonic Reasoning

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Fuzzy Temporal Non-Monotonic Reasoning

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Abstract— non-monotonic reasoning is undecidable. An undecided problem has no solution. Fuzzy logic will made undecidable problem into decidable problem. In this paper, Fuzzy non-monotonic reasoning is studied with a twofold fuzzy logic to made undecidable problem in to decidable. Fuzzy truth maintenance system (FTMS) is studied for computation of fuzzy non-monotonic reasoning. Some examples are given.

Keywords—non-monotonic reasoning, fuzzy Sets, twofold fuzzy sets, fuzzy non-monotonic reasoning, FTMS,incomplete knowledge

I. INTRODUCTION

Sometimes Artificial Intelligence(AI) has to deal with incomplete knowledge. If knowledge base is incomplete then the inference is also incomplete. If some knowledge is added to the system than the inference is changes . In non-monotonic logic, if some knowledge is added to system than inference will be changed. Non-monotonic log is undecidable. Fuzzy logic will made undecidable into decidable. in non-monotonic reasoning. if additional information is added, the reasoning will be changed or jumping conclusion [4].

X is bird Λ x has wings Λ x is known to fly \rightarrow x can fly Suppose,

x is bird Λ x has wings Λ x is unknown to fly \rightarrow x can fly or

x is bird Λ x has wings Λ x is unknown to fly \rightarrow x can't fly For example,

Ozzie is bird Λ Ozzie has wings Λ Ozzie x is known to fly \rightarrow Ozzie can fly

Ozzie is bird Λ Ozzie has wings Λ Ozzie x is unknown to fly \rightarrow Ozzie can't fly

Ozzie is bird Λ Ozzie has wings Λ Ozzie is unknown to fly \rightarrow Ozzie can fly

Consider the formula,

 $\forall x P(x) \land \forall x Q(x) \land \forall x R(x) \Rightarrow \forall x S(x)$

The monotonic logic is given by

 $\forall x \text{ bird}(x) \Lambda \forall x \text{ Wings}(x) \Lambda \forall x \text{ known-to-fly}(x) \rightarrow \forall x \text{ fly}(x)$

Inference S is changed if R is changed. The non-monotonic logic is given by

 $\forall x \text{ bird}(x) \land \forall x \text{ Wings}(x) \land \forall x \text{ unknown-to-fly}(x) \rightarrow \forall x \text{ can-fly}(x) \text{ or } \forall x \text{ can't-fly}(x)$

The conclusion will be changed if added some knowledge in non-monotonic logic. These problems fall under undecided. The undecided problems have no solution. Fuzzy logic will made undecidable problems in to decidable

There are many theories [1] to deal with incomplete information like Probability, Dempster- Shaffer theory, Possibility, Plausibility etc. Zadeh [14] fuzzy logic is based on belief rather than probable (likelihood). The fuzzy logic made imprecise information in to precise.

Zadeh fuzzy logic is defined with single membership function.

The possibility set may be defined for the proposition of the type "x is P" as

$$\pi_P(x) \rightarrow [0,1]$$

 $\pi_P(x) = \max\{ \mu_P(x_i) \}, x \in X$

$$\begin{split} & \mu_P(x) = \mu_P(x_1)/x_1 + \mu_P(x_2)/x_2 + \ldots + \mu_P(x_n)/x_n \\ & \mu_{bird}(x) = \mu_{bird}(x_1)/x_1 + \mu_{bird}(x_2)/x_2 + \ldots + \mu_{bird}(x_n)/x_n \end{split}$$

 $\begin{array}{lll} \mu_{bird}(x) = \mu_{bird}(x_1)/x_1 + \mu_{bird}(x_2)/x_2 + \ldots + \mu_{bird}(x_n)/x_n \\ \mu_{bird}(x) = & 0.1/Penguin + 0.3/Hen + 0.5/Cock + 0.6/Parrot + 0.8/eagle + 1.0/flamingos \end{array}$

Fuzzy logic with two membership functions will give more information

Two fold fuzzy logic P=(A, B) for the proposition of the type "x is P".

P may be considered as

P={belief, disbelief}, {True, false}, {unknown, known}, {belief, disbelief} etc.

$$\begin{array}{l} \mu_P(x) \; \Lambda \; \mu_Q(x) \; \boldsymbol{\rightarrow} \; \mu_S(x) \\ \mu_P(x)^{(unknown, \; known)} \Lambda \; \mu_Q(x) \; ^{(unknown-, \; known)} \; \boldsymbol{\rightarrow} \; \mu_S(x) \; ^{(unknown, \; known)} \\ \text{where P,Q and } \; S \; \text{are twofold fuzzy set known, } \; known \}. \end{array}$$

$$\begin{array}{c} \mu_{bird}(x) \; \Lambda \; \mu_{wings}(x) \; \boldsymbol{\rightarrow} \; \mu_{fly}(x) \\ \mu_{bird}(x)^{(unknown,known)} \Lambda \mu_{wings}(x)^{(unknown-,known)} \boldsymbol{\rightarrow} \mu_{fly}(x)^{(unknown,known)} \end{array}$$

The conflict of the incomplete information may be defend by fuzzy certainty factor(FCF).

FCF =unknown- known)

$$\mu_{\text{bird}}^{\text{ FCF}}(x) \wedge \mu_{\text{wings}}^{\text{ FCF}}(x) \rightarrow \mu_{\text{fly}}^{\text{ FCF}}(x)$$

Where known and unknown are the fuzzy membership functions.

The fuzzy non-monotonic reasoning will bring uncertain knowledge in to certain knowledge.

$$\begin{array}{ccc} \mu_{P}(x) \xrightarrow{(unknown, \, known)} \Lambda \; \mu_{Q}(x) \xrightarrow{(unknown-, known)} \boldsymbol{\rightarrow} \; \mu_{S}(x) \\ S = \; \mu_{S} \xrightarrow{FCF} (x) = 1 & \; \mu_{S} \xrightarrow{FCF} (x) \leq \alpha, \\ 0 & \; \mu_{S} \xrightarrow{FCF} (x) > \alpha \end{array}$$

$$\begin{array}{c} \mu_{bird}(x) \stackrel{(unknown, \, known)}{\Lambda} \, \mu_{wings}(x) \stackrel{(unknown-, known)}{} \boldsymbol{\rightarrow} \\ \mu_{fly}(x) \\ fly = \mu_{fly} \stackrel{FCF}{}(x) = 1 \quad \mu_{fly} \stackrel{FCF}{}(x) \leq \alpha, \\ 0 \quad \mu_{fly} \stackrel{FCF}{}(x) > \alpha \end{array}$$

Fly for 1 and can't fly for 0

Quasi-fuzzy set

A quasi-fuzzy set is defined for the proposition "x is P" as $\mu_P(x) \rightarrow (0, 1)$

III. FUZZY CONDITIONAL INFERENCE

The fuzzy rules are of the form "if <Precedent Part> then <Consequent Part>"

if x is P the n x is Q.

or

. if $x ext{ is } P_1 ext{ and } x ext{ is } P_2 ext{ } x ext{ is } P_n ext{ then } x ext{ is } Q$

The Zadeh [13] fuzzy conditional inference s given by if x is P_1 and x is P_2 x is P_n then x is $Q = \min 1$, $(1-\min(\mu_{P1}(x), \mu_{P2}(x), ..., \mu_{Pn}(x)) + \mu_{Q}(x)$ (2.1)

The Mamdani [8] fuzzy conditional inference s given by if
$$x$$
 is P_1 and x is P_2 x is P_n then x is $Q = \min \{\mu_{P1}(x), \mu_{P2}(x), ..., \mu_{Pn}(x), \mu_{Q}(x)\}$ (2.2)

Reddy [10] The fuzzy conditional inference "Consequent Part" is derived from "Precedent Part".

if
$$x$$
 is P_1 and x is P_2 x is P_n then x is $Q = ix$ is P_1 and x is P_2 x is P_n

Fuzzy conditional inference is given by using mamdani fuzzy conditional inference

$$= \min(\mu_{P1}(x), \, \mu_{P2}(x), \, \dots, \, \mu_{Pn}(x)) \tag{2.3}$$

For instance, x is bird Λ x has wings \rightarrow x can fly x can fly= x is bird Λ x has wings

Quasi-fuzzy set

A quasi-fuzzy set is defined for the proposition "x is P" as

$$\begin{array}{l} \mu_P(x) \rightarrow (0, 1) \\ \mu_{fly}(x) \stackrel{(can, \ can't)}{\longrightarrow} (0, 1) \end{array}$$

IV. THE TWO FOLD FUZZY LOGIC

Zadeh [13] Proposed fuzzy set with single membership function. The two fold fuzzy set [12] will give more evidence than single membership function.

The fuzzy non-monotonic set may defined with two fold membership function using unknown and known

Definition: Given some Universe of discourse X, the proposition "x is P" is defined as its two fold fuzzy membership function as

$$\mu_{P}(x) = {\mu_{P}^{True}(x), \mu_{False}(x)}$$

Interpreting "truth is knkown but false is known", the twofold fuzzy set is given by

$$P = \{\mu_P^{unknown}(x), \, \mu_P^{known}(x)\}$$

Where P is Generalized fuzzy set and $x \in X$,

$$\begin{array}{l} 0 <= \mu_{P}^{unknown}(x) <= 1 \ and, \ 0 <= \mu_{P}^{known}\left(x\right) <= 1 \\ P \ = \ \{ \ \mu_{P}^{unknown}\left(x_{\ 1}\right) \! / \! x_{1} \ + \ldots + \ \mu_{P}^{unknown}\left(x_{\ n}\right) \! / \! x_{n}, \end{array}$$

 $\mu_P{}^{known}(x_1)\!/x_1 \quad + \ldots + \quad \mu_P{}^{unknown}(x_n)\!/x_n, \ x_i \in X, \text{``+''} is \\ union$

For example 'x will fly", fly may be given as Suppose P and Q is fuzzy non-monotonic sets. The operations on fuzzy sets are given below for two fold fuzzy sets.

Negation

$$P' = \{1 - \mu_P^{unknown}(x), 1 - \mu_P^{known}(x) \}/2$$

Disjunction

$$\begin{array}{l} PVQ = \{ \begin{array}{ll} max(\mu_P{}^{known} \ (x) \ , \ \mu_P{}^{known} \ (y)), \ max(\mu_Q{}^{unknown} \ (x) \ , \\ \mu_O{}^{unknown} \ (x)) \} \end{array}$$

Conjunction

$$\begin{array}{lll} P\Lambda Q = \{ & min(\mu_{P}{}^{known} \ (x) \ , \mu_{P}{}^{known} \ (y)), \ min(\mu_{Q}{}^{unknown} \ (x) \ , \\ \mu_{Q}{}^{unknown} (x)) \ \} \end{array}$$

Implication

Zadeh fuzzy conditional inference

P→Q= {min(1, 1-
$$\mu_P^{known}(x) + \mu_Q^{known}(x)$$
, min (1, 1- $\mu_P^{known}(x) + \mu_Q^{known}(x)$ }

Mamdani fuzzy conditional inference

$$P \rightarrow Q = \{ \min(\mu_P^{unknown}(x), \mu_Q^{unknown}(y), \min(\mu_P^{known}(x), \mu_Q^{known}(x)) \}$$

Reddy fuzzy conditional inference

$$P \rightarrow Q = \{ \min (\mu_P^{\text{unknown}}(x), \mu_P^{\text{known}}(y) \} (x,x) \}$$

Composition

PoR = {min_x (
$$\mu_P^{unknown}(x)$$
, $\mu_P^{unknown}(x)$), min_x($\mu_R^{known}(x)$, $\mu_R^{known}(x)$)}

The fuzzy propositions may contain quantifiers like "very", "more or less" . These fuzzy quantifiers may be eliminated as

Concentration

"x is very P

$$\mu_{\text{very P}}(x) = \{ \mu_{\text{very P}}^{\text{unknown}}(x)^2, \mu_{\text{very P}}^{\text{known}}(x)\mu_P(x)^2 \}$$

Diffusion

"x is more or less P"

$$\mu_{more~or~less}~p(x)=(~\mu_{more~or~less}{}^{unknown}~(x)^{1/2},~\mu_{more~or~less}{}^{known}~(x)\mu_P(x)^{0.5}$$

The fuzzy certainty factor (FCF) is defined by fuzziness instead of probability for the fuzzy preposition of the type "x is A"

$$FCF[x, A]=MB[x, A]-MD[x,A],$$

The FCF is the difference between "unknown" and "known" and will eliminate conflict between "unknown" and "known" and, made as single membership function

$$\mu_A^{FCF}(x) = \mu_A^{unknown}(x) - \mu_A^{known}(x)$$

$$\mu_P(x) \rightarrow (0, 1)$$

 $\mu_A \text{ unknown } (x) = 1$

$$\begin{array}{l} \mu_{A}^{FCF}\left(x\right) = 1 - \mu_{A}^{known}\left(x\right) \\ \mu_{fly}^{FCF}\left(x\right) = \left\{1 - \mu_{fly}^{known}(x)\right\} \\ = \left\{1.0/\text{penguin} + 1.0/\text{Ozzie} + 1.0/\text{parrot} + 1.0/\text{waterfowl} + 1.0/\text{eagle} - 0.9/\text{penguin} + 0.7/\text{Ozzie} + .0.3/\text{parrot} + 0.15/\text{waterfowl} + 0.1/\text{eagle}\right\} \\ = \left\{ \begin{array}{l} 0.0/\text{penguin} + 0.1/\text{Ozzie} + .0.7/\text{parrot} + 0.8/\text{waterfowl} + 0.9/\text{eagle} \right\} \\ \text{For instance "} x \ \text{can fly" for } \alpha > = 0.5 \\ \text{Is given as} \\ \left\{ \begin{array}{l} 0.0/\text{penguin} + 0.0/\text{Ozzie} + 1/\text{parrot} + 0.65 \ /\text{waterfowl} + 1/\text{eagle} \right\} \\ \end{array}$$

The inference is given by

Penguin and Ozzie can't fly

Parrot, waterfowl and eagle can fly

V. FUZZY NON-MONOTONIC LOGIC

Fuzzy non-monotonic logic will non-monotonic logic to monotonic logic.

Definition: A default fuzzy set is monotonic set and defined by its quasi-fuzzy set for the proposition "x is P" by

$$\mu_P(x) \rightarrow (0, 1)$$

For instance,

$$\mu_{flv}(x)$$
 (can, can't) \rightarrow (0,1)

Definition: ffuzzy non-monotonic logic is simply two fold fuzzy logic, the non-monotonic proposition may be represented with two fold fuzzy set

$$\mu_{P}(x) = \{\mu_{P}^{\text{unknown}}(x), \mu_{P}^{\text{nunknown}}(x)\}$$

For instance,

$$\mu_{bird}(x) = \{\mu_{bird}^{unknown}(x), \mu_{bird}^{known}(x) \}$$
where $\mu_{P}^{unknown}(x)=1$

$$\begin{array}{ll} \mu_{bird}^{FCF}\left(x\right) &= \left\{1 - \mu_{bird}^{known}\left(x\right)\right\} \\ &= \left\{1.0/penguin + 1.0/Ozzie + 1.0/parrot + 1.0/waterfowl + 1.0/eagle - 0.9/penguin + 0.7/Ozzie + . 0.3/parrot + 0.15/waterfowl + 0.1/eagle \right\} \end{array}$$

= { 0.0/penguin +0.1/Ozzie+ . 0.7/parrot+ 0.8/waterfowl + 0.9/eagle }

$$\begin{array}{l} \mu_{\text{bird}}(x) \ = \{ \ \mu_{\text{bird}} \, ^{\text{unknown} \, (} x), \, \mu_{\text{bird}} \, ^{\text{known} \, (} x) \} \\ \mu_{\text{bird}} ^{FCF}(x) \ = \{ \ 1 \text{-} \, \mu_{\text{bird}} \, ^{\text{known} \, (} x) \} \end{array}$$

if x is P_1 and x is P_2 x is P_n then x is Q if some information is added to the propostion than inference will be changed.

if x is P_1 and x is P_2 \dots x is P_n anx x is P_{n+1} then $\,x$ is $\,Q_1$

x is bird Λ x has wings Λ x is known to fly \Rightarrow x can fly

x is bird Λ x has wings Λ x is unknown to fly \rightarrow x can or can't fly

The two statements combined with two fold fuzzy logic.

$$\begin{array}{l} \mu_{\text{bird}}(x) \ \Lambda \ \mu_{\text{wings}}(x) \Rightarrow \mu_{\text{fly}}(x) \\ \{ \ \mu_{\text{bird}} \ ^{\text{unknown}}(x), \ \mu_{\text{bird}} \ ^{\text{known}}(x) \} \ \Lambda \ \{ \ \mu_{\text{bird}} \ ^{\text{unknown}}(x), \ \mu_{\text{bird}} \ ^{\text{known}}(x) \} \\ \{ \ \mu_{\text{bird}} \ ^{\text{unknown}}(x), \ \mu_{\text{bird}} \ ^{\text{known}}(x) \} \ \Lambda \ \{ \ \mu_{\text{bird}} \ ^{\text{unknown}}(x), \ \mu_{\text{bird}} \ ^{\text{known}}(x) \} \\ \{ \ \mu_{\text{bird}} \ ^{\text{FCF}}(x) \ \Lambda \ \mu_{\text{wings}} \ ^{\text{FCF}}(x) \Rightarrow \mu_{\text{fly}}(x) \\ \text{if} \ x \ \text{is} \ P_1 \ \text{and} \ P_2 \ \dots x \ \text{is} \ P_n \\ = \ \min(\mu_{P1}(x), \mu_{P2}(x), \ \dots, \ \mu_{Pn}(x)) \\ \mu_{\text{fly}}(x) = \mu_{\text{bird}} \ ^{\text{FCF}}(x) \ \Lambda \ \mu_{\text{wings}} \ ^{\text{FCF}}(x) \end{array}$$

$$\begin{array}{l} \mu_{bird}^{FCF}(x) = \{1.0/penguin + 1.0/Ozzie + .\,0.8/parrot + 0.85/waterfowl + 0.9/eagle - 0.9/penguin + 0.8/Ozzie + .\,0.2/parrot + 0.1/waterfowl + 0.05/eagle\,\} \\ = \{0.1/penguin + 0.2/Ozzie + .\,0.6/parrot + 0.75/waterfowl + 0.8/eagle\,\,\} \end{array}$$

$$\begin{array}{l} \mu_{wings}(x) = \{\mu_{wings} \ ^{unknown}(x), \, \mu_{wings} \ ^{unnown}(x)\} \\ \mu_{wings}(x) = 1, \, where \, wngs \, is \, quasi \, fuzzy \, set \end{array}$$

Reddy fuzzy conditional inference "consequent part "may be derived from "precedent part".

$$\begin{array}{l} \mu_P(x) \ \Lambda \ \mu_Q(x) \ \rightarrow \mu_S(x) \\ \mu_S(x) = \mu_P(x) \ \Lambda \ \mu_Q(x) \\ x \ \text{is bird} \ \Lambda \ x \ \text{has wings} \ \rightarrow x \ \ \text{will fly} \\ x \ \text{will fly =min} \ \{ \ x \ \text{is bird} \ , \ x \ \text{has wings} \ \} \end{array}$$

The inference of "x can fly" for $\alpha > = 0.5$ is given by = 1/parrot + 1/waterfowl + 1/eagle

Here fuzzy logic made imprecise information to precise information's. Some birds can fly and some birds can't fly.

The fuzzy decision sets or quasi fyzzy set is defined by

$$R = \mu_A^R(x) = 1 \quad \mu_A^{FCF}(x) \leq \alpha, \\ 0 \quad \mu_A^{FCF}(x) > \alpha$$

The parrot, waterfowl and eagle can fly.

The penguin and Ozzie can't fly

The inference of "x can.t fly" for α <0.5 is given by = 0/.1penguin +0.2/Ozzie

The inference of "x can fly" for $\alpha \ge 0.5$ is given by = 0.6/parrot+ 0.75/waterfowl + 0.8/eagle

he parrot, waterfowl and eagle can fly and, penguin and Ozzie are can't fly.

A. Fuzzy Temporal Non-Monotonic Logic Temporal databases may be non-monotonic in nature. When time changed than implication changes.

Condiger the temporal database

Fno	То	D
F101	Colombo	23.30
F201	Hong Kong	1.40
F301	New York	9.20

F402	Kuala	11.50
F502	Lumpur Frankfort	21.45
F101	Dubai	8.30

The flight will be available with in right depature time otherwise not available.

Consider fuzzy temporal database

Fno	To	D	late
F101	Colombo	23.30	0.2
F201	Hong Kong	1.40	0.0
F301	New York	9.20	0.6
F402	Kuala Lumpur	11.50	0.2
F502	Frankfort	21.45	0.5
F101	Dubai	8.30	0.6

late=(unknown time -known-time)

VI. FUZZY TRUTH MAITANACE SYSTEM

Doyel [4] studied truth maintenance system TMS] for non-monotonic reasoning

The fuzzy truth maintenance system (FTMS) for fuzzy non-monotonic reasoning using fuzzy conditional inference as

if x is x is P_1 and P_2 And x is P_n then Q

 $=\min(\mu_{P1}(x), \mu_{P2}(x), ..., \mu_{Pn}(x))$

FTMS is having There is list of justification and conditions.

if x is bird and x has wings then x can fly

List L(IN-node, OUT-node)
IN node is undeciable information.

OUT node is decidable information.

L1 bird(unknown,known)

L2 wings(unknown-, known)

The concequent part derived from precedent patrt i.e, fly

The FTMS gives using FCF

IN

L1 bird(1, 0.3)

L2 wongs(1, 0.4)

OUT

Fly= min{0.7, 0.6}=0.6 fly if FCF>0.5

The FTMS gives using FCF

IN

L1 bird(1, 0.5)

L2 wongs(1, 0.6)

OUT

Fly= $min\{05,0.4\}=0.6$

can' fly if FCF<0.5

in the case of parrot, waterfowl and agle can fly in case of Penguin and Ozzie can't fly.

Here the fuzzy nonmonotonic logic is making uncertainty to certainty.

Consiser another example,

"Raju and Rani are in the house. There is gun. Rani died with gun shot." Whether Raju shot at Rani or Rani shot herself.

if x is shoot her and x is shoot by herself and investigation then x is killed

The FTMS gives using FCF

L1 shoot-by-herself(1, 0.7)

L2 shot her(1, 0.6)

L2 investigation(1, 0.8)

killed= min{3, 0.4,0.2}=02

Not killed if FCF<0.5

The FTMS gives using FCF

L1 shoot-by-herself(1, 0.3) L2 shot her(1, 0.4)

L2 investigation(1, 0.2)

killed= min{0.7,0.6,0.8}=0.6

killed if FCF>=5

VII. FUZZY MODULATIONS AND LOGIC PROGRAMMING

The fuzzy reasoning system(FRS) is complex reasoning system for incomplete AI problem solving. The fuzzy predicate logic (FPL) is modulating transform fuzzy facts and rules in to meta form(semantic form). These fuzzy facts and rules are modulated to represent the knowledge available to the incomplete problem [17].

The fuzzy modulations for Knowledge representation are type of modules for fuzzy propositions "x is A".

"x is A" is may be represented as

[A]R(x),

where A is twofold fuzzy set {unknown, known}, R is relation and x is individual in the Unversed of discourse X.

For instance

"x is bird" is modulated as

[bird]is(x)

The FPL is e combined with logical operators.

Let A and B be two fold fuzzy sets.

x is ¬A

 $[\neg A]R(x)$

x is A or x is B

[A V B]R(x)

x is A and x is B

 $[A \Lambda B]R(x)$

if x is A then x is B

 $[A \rightarrow B]R(x)$

x is bird

[bird]is(x)

if x is bird then x can fly

if [bird]is(x) then [fly]is(x)

or

 $[bird] \rightarrow [fly] is(x)$

if x is bird and x has wings then x can fly if $[bird]is(x)\Lambda[wings]has[x]$ then [fly]can(x)

 $\begin{array}{ll} \mbox{if } x \mbox{ is } x \mbox{ is } P_1 \mbox{ and } P_2 \mbox{} \mbox{ And } x \mbox{ is } P_n \mbox{ then } Q &= \{ \mbox{ $\mu_Q(x)$} \} \\ \mbox{if } [\mbox{bird}] \mbox{is}(x) \Lambda[\mbox{wings}] \mbox{has}[x] & \mbox{then } [\mbox{fly}] \mbox{can}(x) \\ [\mbox{fly}] \mbox{can}(x) = \{ [\mbox{bird}] \mbox{is}(x) \Lambda[\mbox{wings}] \mbox{has}[x] \\ \end{array}$

The Logic Programming may be written in SWI-Prolog

as

fuzzy(Ozzie, A,B, M) :- A < B, M is A.

fuzzy(Ozzie, A,B, M) :- $A \ge B$, M is B.

fuzzy(C,M,F):-C<M,F is C.

fuzzy(C,M,F):-C>=M F is M.

fuzzy(X, A,B,C,F) :- fuzzy(X, A,B,M), fuzzy(C,M,F). ?-run(X,0.8,0.7,0.64,F).

F=0.64

If F >= 6, Ozzie can fly ?-run(Ozzie, 0.6, 0.5, 0.4, F).

F=0.4

If F <6, Ozzie can't fly

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