

Modeling the H-Index Based on the Total Number of Citations and the Duration from the First Publication

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Abstract. The productivity of researchers and the impact of the work they do is a preoccupation of universities, research funding agencies and sometimes even researchers themselves. The *h*-index is the most popular of different metrics to measure these activities. This research deals to present a practical approach to model the *h*-index based on the total number of citations and the duration from the publishing of the first article. To determine the effect of every factor (C and D) on H, we applied a set of simple nonlinear regression. The results indicated that both C and D had significant effect on H (p<0.001). The

power of these equations to estimate of *H* was 93.4% and 39.8%, respectively, that verified the model based on C had a better fit. Then, to investigate the simultaneous effects of C and D on H, multiple nonlinear regression were applied. The results indicated that C and D had significant effect on H (p<0.001). Also, the power of this equation to estimate of *H* was 93.6%. Finally, to model and estimate the *h*-index, *h*, as a function of C and D, the multiple nonlinear quartile regression was used. The goodness of fitted model also was also assessed.

Keywords: H-index, Citation, Duration, Modelling, Relationship, Regression.

1. Introduction

The productivity of researchers and the impact of the work they do is a preoccupation of universities, research funding agencies and sometimes even researchers themselves. Various metrics have been used to measure these including journal impact factors, citation counts and publication rates. At present, however, the *h*-index is the most popular of these metrics (Hirsch, 2005; Braun et al., 2006; Schubert and Glänzel, 2007; Harzing and van der Wal, 2009). Hirsch's definition of the index is that h = m if m of a researcher's p papers have at least m citations each and each of the other papers has no more than m citations. As a guide, Hirsch (2005) suggested that a 'successful' scientist would have h = 20 after 20 years of work, whereas outstanding and 'truly unique' individuals would have h = 40 and h = 60, respectively, after 20 years of work. Subsequent work has shown that this is too great a generalisation, if only because h is highly discipline-specific and depends on circumstance, the comprehensiveness of the literature databases used to calculate the index and many other factors (Vinkler, 2007; Ruch and Ball, 2010). For example, very eminent mathematicians often have h < 10 and some Nobel laureates also have very small *h*-indices (Yong, 2014). The inevitable inference is an individual's *h*-index should be considered in the context of these factors and of the distribution of h for a given number of papers and citations appropriate to the individual researcher. Some researchers

introduced alternative versions of the h-index (Bar-Ilan, 2010). Generally, all of the given indices consider the number of citations received by articles. Recently, scientists have studied and developed theoretical models to estimate and model these indices based on other indicators, for example based on the total number of citations C (Hirsch, 2005), based on the total number of publications T (Egghe and Rousseau, 2006), based on the total number of publications with minimum one citation T_1 (Burrell 2013a), based on C and T (Glänzel, 2006; Iglesias and Pecharroman, 2007; Schubert and Glänzel, 2007; Bletsas and Sahalos, 2009; Egghe et al., 2009; Egghe and Rousseau, 2012), based on C, T_1 and the total number of citations for the 1 most cited papers C₁ (Bertoli-Barsotti and Lando, 2015). Burrell (2013b) and Bertoli-Barsotti and Lando (2015) respectively applied standard and shifted geometric distribution to predict and estimate the h-index of scientists. Bertoli-Barsotti and Lando (2017a) empirically studied the basic and improved Lambert-*W* formula for estimating the *h*-index and compare them with the well-known previous models. Bertoli-Barsotti and Lando (2017b) presented a new formula to estimate the *h*-index when we do not have information about the whole set of citation dataset.

This research deals to present a practical approach to model the h-index based on the total number of citations and the duration from the publishing of the first article

2. Methodology

This section is devoted to discuss about details of data collection, samples and statistical techniques that have applied to analyze dataset.

2.1. Data Collection

The dataset of this research contains the information of articles for 29470 Iranian scientists that have indexed in Google Scholar.

2.2. Data Analysis

Statistics, data analysis and data mining are popular approaches to extract knowledge from dataset. The data gathered from the Google Scholar were fed and analyzed using the SPSS 25, and R 3.3.2 software. First, the descriptive statistics about the values of *h*-index, C and D is provided.

To determine the effect of every factor (C and D) on H, we applied a set of simple nonlinear regression. Also to investigate the simultaneous effects of C and D on H, multiple nonlinear regression were applied. Finally, to model and estimate the *h*-index based on C and D, the multiple nonlinear quartile regression (MNLQR) was used. The goodness of fitted model also was assessed by the coefficient of determination (R^2), and comparing actual values with predicted values.

2.2.1. Simple Nonlinear Regression

To model a quantitative response variable Y based on a predictor variable X, simple nonlinear regression (SNLR) model is a powerful technique. The general equation of SNLR is presented by

$$Y = \beta_0 + \beta_1 X^{\beta_2} + \boldsymbol{\varepsilon}_1$$

where β_0 , β_1 and β_2 are model parameters (coefficients) and ε is the random components of the model which follow independent normal distribution. The estimated equation of SLR model is presented by

$$\widehat{Y} = b_0 + b_1 X^{b_2},$$

where, b_0 , b_1 , b_2 and \hat{Y} are estimations of β_0 , β_1 , β_2 , and Y, respectively.

2.2.2. Multiple Nonlinear Regression

To model a quantitative response variable Y based on predictor variables $X_1, ..., X_k$, multiple nonlinear regression (MNLR) is a powerful technique. The general equation of MNLR with two predictors X_1 and X_2 is presented by

$$Y = \beta_0 + \beta_1 X_1^{\ \beta_2} + \beta_3 X_2^{\ \beta_4} + \beta_5 X_1^{\ \beta_6} X_2^{\ \beta_7} + \varepsilon_4$$

where $\beta_0, ..., \beta_7$ are model parameters (coefficients) and $\boldsymbol{\varepsilon}$ is the random components of the model which follow independent normal distribution. The estimated equation of MNLR model is also presented by

$$\hat{Y} = b_0 + b_1 X_1^{\ b_2} + b_3 X_2^{\ b_4} + b_5 X_1^{\ b_6} X_2^{\ b_7},$$

where $b_0, ..., b_7$ are estimations of $\beta_0, ..., \beta_7$, and \hat{Y} is the estimated value of Y.

2.2.3. Multiple Nonlinear Quartile Regression

In multiple nonlinear quartile regression (MNLQR), first the quartiles of response variable have been computed. Then, based on the values of quartiles, the observations categorized in 4 distinct categories. Finally, a separate MNLR is run, on each category.

3. Results

The descriptive statistics of research variables contained C and D is given the first subsection. The Subsection 2 reports the SNLR results to predict the separate effects of every factor (C and D) on h. The Subsection 3 is regards to MNLR results to investigate the simultaneous effects of C and D on H. The Subsection 4 reports the MNLQR results to model the effects of factors on h, in each quartile.

3.1. Descriptive Statistics

The descriptive statistics of research variables contained minimum, maximum, mean, standard deviation, and quartiles are summarized in Table 1. As Table 1 indicates the means of h, C and D

for Iranian scientists are 5.74, 248.78, and 7.98, respectively. Also, the value of *h* for at least 25%, 50% and 75% of them is at most 2 (Q_1 =2), 4 (Q_2 =4), and 7 (Q_3 =7), respectively.

	Mean	Std. Deviation	Minimum	Maximum		Quartile	
					First (Q ₁)	Second (Q ₂)	Third (Q ₃)
h	5.74	5.79	1	84	2.00	4.00	7.00
С	248.78	828.84	1	37570	15.00	58.00	200.00
D	7.98	4.59	1	42	5.00	7.00	10.00

Table 1: Descriptive statistics of research variables

3.2. SNLR Results

This part is regard to study the impact of each factor (C and D) on *h*. In this research, *h* was the response variable. Also the variables C and D were continuous predictors. Tables 2 and 3 summarize the results of SNLR models for the variables C and D. As Table 2 indicates, the C and D factors had significant effect on *h* (p<0.001). Figure 1 also shows the plot of fitted curve with data.



Figure 1: Plot of fitted curve with data SNLR models

Table 3 shows the parameter estimates of SNLR models for C and D, respectively. Based on the results of Table 3, we can estimate the h as a function of C and D, by

$$\hat{h}_C = 0.600C^{0.476}$$

and

$$\hat{h}_D = 0.667 D^{1.041}$$

respectively. Also, the power of these equations to estimate of h is 93.4% and 39.8%, respectively. Figure 2 and Table 4 show the plot of actual values versus predicted values and the correlations between them. As can be seen the SNLR model based on C had a better fit.

Factor	Source	Sum of Squares	df	Mean Squares	F	R ²	р
	Regression	1892965	2	946482.5	429143.66	0.934	< 0.001
	Residual	64992.09	29468	2.205514			
С	Uncorrected Total	1957957	29470				
	Corrected Total	987069.3	29469				
	Regression	1364231	2	682115.4	33854.95	0.398	< 0.001
	Residual	593726.3	29468	20.14817			
D	Uncorrected Total	1957957	29470				
	Corrected Total	987069.3	29469				

Table 2: The results of SNLR models to study the effect of C and D on h

Table 3: The parameter estimates of SNLR models for C and D

Factor	Parameter	Estimate	Std. Error	95% Confidence Interval		
T detor				Lower Bound	Upper Bound	р
С	b_1	0.600	0.003	0.595	0.606	< 0.001

	<i>b</i> ₂	0.476	0.001	0.474	0.477	<0.001
D	b_1	0.667	0.014	0.640	0.694	<0.001
	<i>b</i> ₂	1.041	0.008	1.025	1.057	<0.001



Figure 2: Plot of actual values versus predicted values

Table 4: Pearson and Spearman correlations between actual values and predicted values

	Spearman's rho		Pearson	
	Correlation Coefficient	р	Correlation Coefficient	р
Predicted Values (based on C)	0.954	<0.001	0.967	<0.001

Predicted Values (based on D)	0.779	<0.001	0.632	<0.001
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3.3. MNLR Results

This part is regard to study the simultaneous impacts of C and D on *h*. Tables 5 and 6 summarize the results of MNLR model. As Table 5 indicates, the C and D factors had significant effect on H (p<0.001). Table 6 shows the parameter estimates of MNLR model.

Table 5: The results of MNLR model to study the effect of C and D on h

Factor	Source	Sum of Squares	df	Mean Squares	F	\mathbb{R}^2	р
	Regression	1895013.156	7	270716.1652	126717.88	0.936	< 0.001
	Residual	62943.8438	29463	2.136369134			
C, D	Uncorrected Total	1957957	29470				
	Corrected Total	987069.2904	29469				

Based on the results of Table 6, we can estimate the *H* as a function of C and D, by

$$\hat{h}_{CD} = 0.673C^{0.419} - 0.183D^{0.939} + 0.129C^{0.424}D^{0.370}.$$

Also, the power of this equation to estimate of *h* is 93.6% that is not significantly more than 93.4% (\hat{h}_c). Figure 3 and Table 7 show the plot of actual values versus predicted values and the correlations between them. As can be seen the MNLR model can nicely estimate the values of *h*.

Table 6: The parameter estimates of MNLR model

Parameter	Estimate	Std. Error	95% Confidence Interval	

			Lower Bound	Upper Bound	р
<i>b</i> ₁	0.673	0.020	0.633	0.712	<0.001
<i>b</i> ₂	0.419	0.014	0.392	0.445	<0.001
<i>b</i> ₃	-0.183	0.028	-0.238	-0.128	<0.001
b_4	0.939	0.061	0.819	1.058	<0.001
<i>b</i> ₅	0.129	0.028	0.073	0.184	<0.001
<i>b</i> ₆	0.424	0.027	0.372	0.477	<0.001
<i>b</i> ₇	0.370	0.084	0.206	0.534	<0.001



Figure 3: Plot of actual values versus predicted values

Table 7: Pearson and Spearman	correlations between actual	values and predicted values
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Spearman's rho	Pearson

	Correlation Coefficient	р	Correlation Coefficient	р
Predicted Values (based on C and D)	0.968	<0.001	0.953	<0.001

3.4. MNLQR Results

This part is regard to study the simultaneous impacts of C and D on different quartiles of *h*. We divide the observations in 4 groups as follow: First group: Observations with $h \le 2$; Second group: Observations with $2 < h \le 4$; Third group: Observations with $4 < h \le 7$; Fourth group: Observations with h > 7. Based on the results of Table 8, we can conclude that the C and D factors had significant effect on *h* (p<0.001), in every category. Based on the results, the *h* can be estimated as a function of C and D, by

$$\hat{h}_{C,D} = b_1 C^{b_2} + b_3 D^{b_4} + b_5 C^{b_6} D^{b_7},$$

in categories 1 to 4, respectively.

Category	Parameter	Estimate	Std. Error	95% Confidence Interval		
				Lower Bound	Upper Bound	р
1	<i>b</i> ₁	.929	.010	.909	.948	<0.001
	<i>b</i> ₂	.230	.008	.214	.246	<0.001
	<i>b</i> ₃	.104	.020	.064	.144	<0.001
	b_4	.813	.079	.658	.968	<0.001
	b_5	057	.015	087	027	<0.001
	<i>b</i> ₆	.322	.020	.284	.361	<0.001

Table 8: The parameter estimates of MNLQR model

	<i>b</i> ₇	.729	.079	.574	.883	< 0.001
	<i>b</i> ₁	11.837	322.351	-620.073	643.748	< 0.001
	<i>b</i> ₂	.211	1.558	-2.844	3.266	<0.001
	<i>b</i> ₃	-4.951	14.521	-33.416	23.514	<0.001
	<i>b</i> ₄	.021	.182	335	.377	<0.001
	<i>b</i> ₅	-5.983	335.988	-664.626	652.661	< 0.001
	<i>b</i> ₆	.288	1.739	-3.122	3.698	< 0.001
2	<i>b</i> ₇	006	.256	508	.496	<0.001
	<i>b</i> ₁	1.682	.191	1.307	2.057	< 0.001
	<i>b</i> ₂	.319	.036	.247	.390	< 0.001
	<i>b</i> ₃	.082	.194	297	.462	<0.001
3	b_4	.554	.564	552	1.659	< 0.001
	<i>b</i> ₅	069	.051	168	.030	< 0.001
	<i>b</i> ₆	.672	.057	.561	.783	< 0.001
	<i>b</i> ₇	.093	.036	.022	.164	< 0.001
	<i>b</i> ₁	.414	.032	.352	.476	< 0.001
	<i>b</i> ₂	.523	.009	.505	.541	<0.001
	<i>b</i> ₃	4.709	.643	3.449	5.969	< 0.001
4	<i>b</i> ₄	494	.101	693	295	< 0.001
	<i>b</i> ₅	001	.001	003	.000	<0.001
	<i>b</i> ₆	1.275	.055	1.167	1.383	< 0.001
	<i>b</i> ₇	-1.348	.148	-1.637	-1.059	<0.001

4. Conclusion

This research dealt to present a practical approach to model the h-index (h) based on the total number of citations (C) and the duration from the publishing of the first article (D). To

determine the effect of every factor (C and D) on *h*, we applied a set of simple nonlinear regression. The results indicated that both C and D had significant effect on *h* (p<0.001) and we can estimate the *h* as a function of C and D, by

$$\hat{h}_{C} = 0.600C^{0.476}$$
,

and

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respectively. Also, the power of these equations to estimate of h was 93.4% and 39.8%, respectively, that verified the model based on C had a better fit.

Then, to investigate the simultaneous effects of C and D on *h*, multiple nonlinear regression were applied. The results indicated that C and D had significant effect on *h* (p<0.001) and we can estimate the *h* as a function of C and D, by

$$\hat{h}_{C,D} = 0.673C^{0.419} - 0.183D^{0.939} + 0.129C^{0.424}D^{0.370}.$$

Also, the power of this equation to estimate of *H* was 93.6% that is not significantly more than 93.4% (\hat{h}_{c}).

Finally, to model and estimate the h, as a function of C and D, the multiple nonlinear quartile regression was used. The goodness of fitted model also was also assessed.

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